

# Search for extra Higgs bosons at ILC after LHC

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Based on Shinya Kanemura, Hiroshi Yokoya and YJZ, arXiv: 1404.5835

## Outline

- Motivation
- Extra Higgs bosons within two Higgs doublet models (2HDM)
- Hadron collider reach for 2HDM particles
- Complementary discovery reach of extra Higgs bosons at ILC
- Summary

## Motivation



Photo: A. Mahmoud  
François Englert



Photo: A. Mahmoud  
Peter W. Higgs

The Nobel Prize in Physics 2013 was awarded jointly to François Englert and Peter W. Higgs *"for the theoretical discovery of a mechanism that contributes to our understanding of the origin of mass of subatomic particles, and which recently was confirmed through the discovery of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN's Large Hadron Collider"*

- If the standard model (SM) electroweak theory is non-minimal, it is natural to consider extensions of Higgs sector.
- LHC discovery potential for extra Higgs bosons is limited in the relatively small  $\tan\beta$  region.
- ILC may provide interesting signatures as a complementary machine of LHC

## 2 Higgs doublet extensions of SM

- T.D. Lee, *A Theory of Spontaneous T Violation*, Phys. Rev. **D8**, 1226 (1973).

The first motivated 2HDM: an attempt to find a new source of CP-violation.

- S.L. Glashow and S. Weinberg, *Natural Conservation Laws For Neutral Currents*, Phys. Rev. **D15**, 1958 (1977).

To avoid neutral-Higgs-mediated tree-level flavor changing neutral currents (FCNCs), all fermions of a given electric charge can couple to at most one Higgs doublet (in a model with multiple scalar doublets).

- N.G. Deshpande and E. Ma, *Pattern Of Symmetry Breaking With Two Higgs Doublets*, Phys. Rev. **D18**, 2574 (1978).

Parameters of the Higgs potential had to lie in an appropriate region of parameter space to ensure that  $U(1)_{EM}$  is not broken.

- the axion as the CP-odd scalar of a 2HDM [the Peccei-Quinn mechanism].
- the requirement of a second Higgs doublet in the minimal supersymmetric extension of the Standard Model (MSSM).

Related  
History

## 2HDM particle content

Two Higgs doublet fields:

$$\Phi_i = \begin{pmatrix} H_i^+ \\ (H_i^0 + iA_i^0)/\sqrt{2} \end{pmatrix}, \quad i = 1, 2.$$

General Higgs potential:

$$V_{2\text{HDM}} = m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[ m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] \quad \boxed{\text{Gunion \& Haber (2003)}} \\ + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \left[ \lambda_6 (\Phi_1^\dagger \Phi_1) + \lambda_7 (\Phi_2^\dagger \Phi_2) \right] (\Phi_1^\dagger \Phi_2) + \text{h.c.} \right\}.$$

hypercharge  
 $Y=1$

After SSB: 5 physical Higgs scalar left:

2 CP-even    1 CP-odd    2 Charged

$h, H$

$A$

$H^\pm$

## General 2HDM structure

different Higgs-fermion interactions

- Type I: one Higgs doublet couples to both up-type and down-type fermions, and the other Higgs doublet does not couple at all to the fermions. (Haber, Kane & Sterling (1979))
- Type II: one doublet couples only to down-type quarks and another doublet couples to the up-type quarks. (Donoghue & Li (1979))
- Type III: all possible Higgs-fermion couplings allowed. (Cheng & Sher (1987))
- Lepton-specific / flipped / neutrino-specific / inert...

Gunion, Haber, Kane & Dawson (2000);  
Branco, Ferreira, Lavoura, Rebelo, Sher & Silva (2011)

# Search for extra Higgs bosons at ILC after LHC

## basic experimental constraints on 2HDM

rho parameter  $\sim 1$ : The experimental value of the rho parameter is quite close to unity

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = \frac{\sum_i [T_i(T_i + 1) - Y_i^2] v_i^2}{\sum_i 2Y_i^2 v_i^2}$$

$Y_i$  : hypercharge  
 $T_i$  : isospin  
 $v_i$  : VEV

EW sector of the model would approximately have a global SU(2) symmetry (the custodial symmetry) to guarantee  $\rho=1$  at tree level

Custodial SU(2) symmetry exists in the kinetic term

- Standard Model
- Models with multi-doublet fields (with singlets)

Flavor changing neutral current (FCNC):

- SM: suppressed by electromagnetic gauge symmetry and GIM
- 2HDM: imposing discrete Z2 symmetry

# Search for extra Higgs bosons at ILC after LHC

## 2HDM Yukawa interactions

with softly broken  $Z_2$  symmetry

$$\mathcal{L}_{\text{yukawa}}^{\text{2HDM}} = - \sum_{f=u,d,\ell} \left( \frac{m_f}{v} \xi_h^f \bar{f} f h + \frac{m_f}{v} \xi_H^f \bar{f} f H - i \frac{m_f}{v} \xi_A^f \bar{f} \gamma_5 f A \right)$$

neutral Higgs

$$- \left\{ \frac{\sqrt{2} V_{ud}}{v} \bar{u} (m_u \xi_A^u P_L + m_d \xi_A^d P_R) d H^+ + \frac{\sqrt{2} m_\ell \xi_A^\ell}{v} \bar{\nu}_L \ell_R H^+ + \text{H.c.} \right\}$$

charged Higgs

	$\Phi_1$	$\Phi_2$	$u_R$	$d_R$	$\ell_R$	$Q_L$	$L_L$
Type-I	+	-	-	-	-	+	+
Type-II	+	-	-	+	+	+	+
Type-X	+	-	-	-	+	+	+
Type-Y	+	-	-	+	-	+	+

mixing factors:

4 types	$\xi_h^u$	$\xi_h^d$	$\xi_h^\ell$	$\xi_H^u$	$\xi_H^d$	$\xi_H^\ell$	$\xi_A^u$	$\xi_A^d$	$\xi_A^\ell$
Type-I	$c_\alpha/s_\beta$	$c_\alpha/s_\beta$	$c_\alpha/s_\beta$	$s_\alpha/s_\beta$	$s_\alpha/s_\beta$	$s_\alpha/s_\beta$	$\cot \beta$	$-\cot \beta$	$-\cot \beta$
Type-II	$c_\alpha/s_\beta$	$-s_\alpha/c_\beta$	$-s_\alpha/c_\beta$	$s_\alpha/s_\beta$	$c_\alpha/c_\beta$	$c_\alpha/c_\beta$	$\cot \beta$	$\tan \beta$	$\tan \beta$
Type-X	$c_\alpha/s_\beta$	$c_\alpha/s_\beta$	$-s_\alpha/c_\beta$	$s_\alpha/s_\beta$	$s_\alpha/s_\beta$	$c_\alpha/c_\beta$	$\cot \beta$	$-\cot \beta$	$\tan \beta$
Type-Y	$c_\alpha/s_\beta$	$-s_\alpha/c_\beta$	$c_\alpha/s_\beta$	$s_\alpha/s_\beta$	$c_\alpha/c_\beta$	$s_\alpha/s_\beta$	$\cot \beta$	$\tan \beta$	$-\cot \beta$

fermionphobic

MSSM

leptonphobic  
(small  $\tan \beta$ )

leptonphilic  
(large  $\tan \beta$ )

completeness

$$c_\alpha \sim \cos$$

$$s_\beta \sim \sin$$

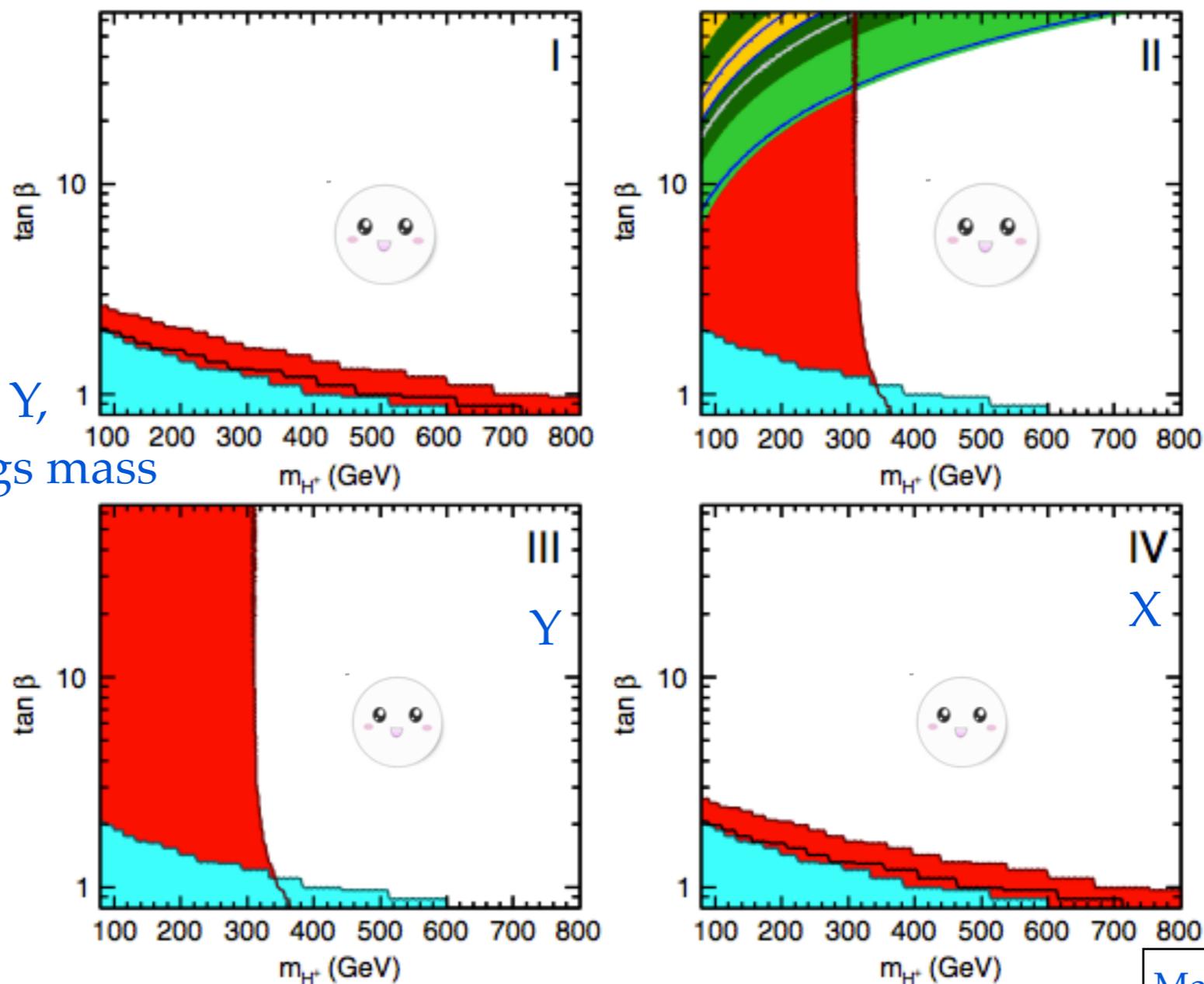
$$v = \sqrt{v_1^2 + v_2^2} \simeq 246 \text{ GeV}, \quad \tan \beta = v_2/v_1,$$

when  $\sin(\beta - \alpha) = 1$ .  $h$  is SM Higgs

Aoki, Kanemura, Tsumura and Yagyu, 2009

# Search for extra Higgs bosons at ILC after LHC

## Flavor constraints on charged Higgs boson



most  
constrained

In type II and type Y,  
still room for large Higgs mass

Mahmoudi & Stal (2010)

FIG. 10 (color online). Excluded regions of the  $(m_{H^+}, \tan\beta)$  parameter space for  $Z_2$ -symmetric 2HDM types. The color coding is as follows:  $\text{BR}(B \rightarrow X_s \gamma)$  (red),  $\Delta_{0-}$  (black contour),  $\Delta M_{B_d}$  (cyan),  $B_u \rightarrow \tau \nu_\tau$  (blue),  $B \rightarrow D \tau \nu_\tau$  (yellow),  $K \rightarrow \mu \nu_\mu$  (gray contour),  $D_s \rightarrow \tau \nu_\tau$  (light green), and  $D_s \rightarrow \mu \nu_\mu$  (dark green). The white region is not excluded by any of these constraints.

# Search for extra Higgs bosons at ILC after LHC

BABAR observes a 3.4 sigma deviation in  $B \rightarrow D\text{-tau-nu}/D^*\text{-tau-nu}$ .  
However, this data is inconsistent with the type II 2HDM at the 99.8% C.L.

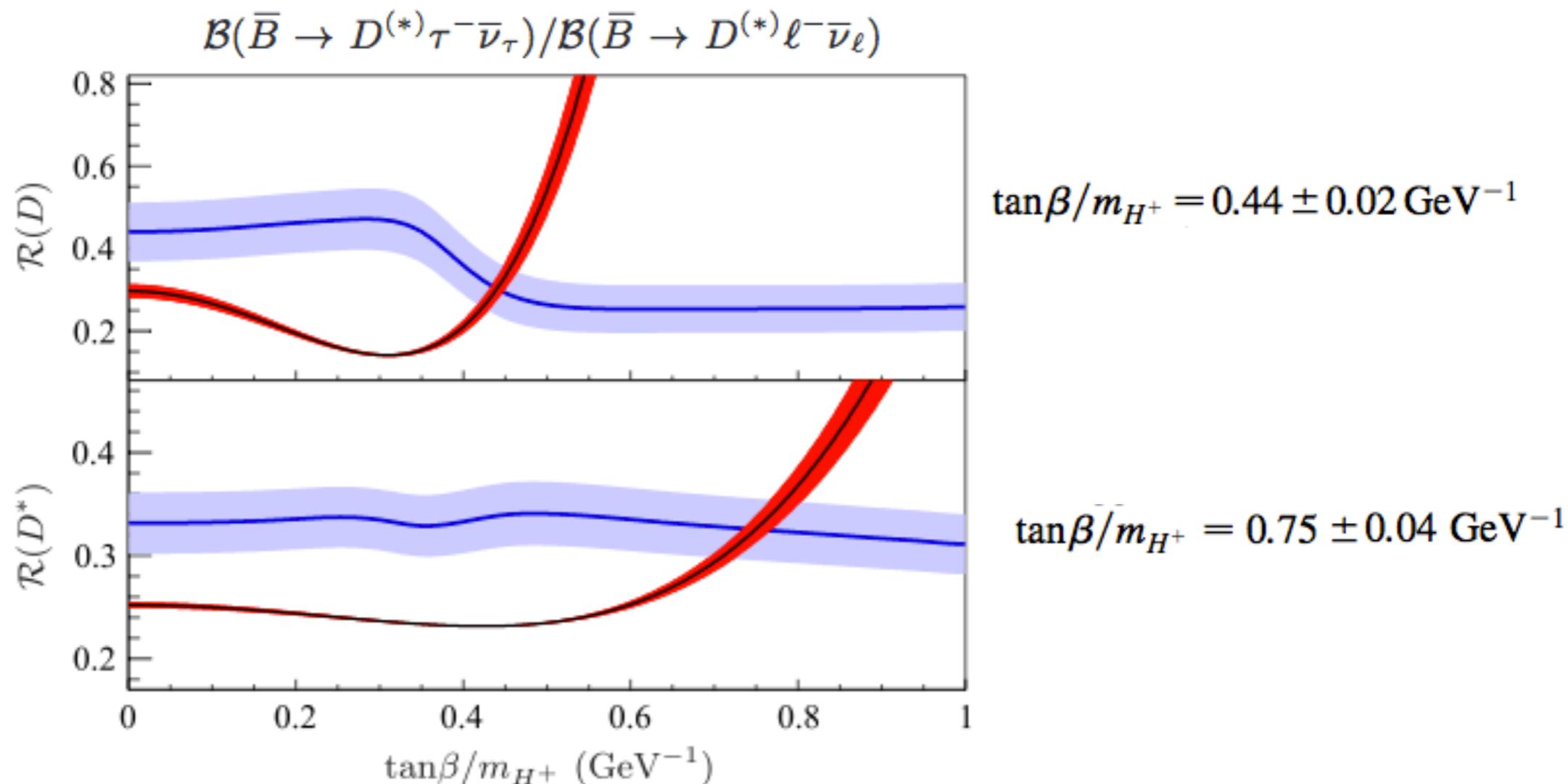


FIG. 2 (color online). Comparison of the results of this analysis (light gray, blue) with predictions that include a charged Higgs boson of type II 2HDM (dark gray, red). The SM corresponds to  $\tan\beta/m_{H^+} = 0$ .

J.P.Lees et al. [BaBar collaboration], Evidence for an excess of  $B \rightarrow D^{(*)}\text{-tau-nu}$  decays, PRL.109,101802

## Extra Higgs boson production at the LHC

### Neutral Higgs bosons production at the LHC

$$\left. \begin{array}{l} \bullet \text{ H, A: } gg \rightarrow H/A \\ \phantom{\bullet \text{ H, A: }} gg(q\bar{q}) \rightarrow Q\bar{Q}H/A \end{array} \right\} H/A \rightarrow b\bar{b} \text{ or } \tau^+\tau^-$$

### Charged Higgs bosons production at the LHC

$$M \leq m_t - m_b \quad gg(q\bar{q}) \rightarrow H^- t\bar{b}$$

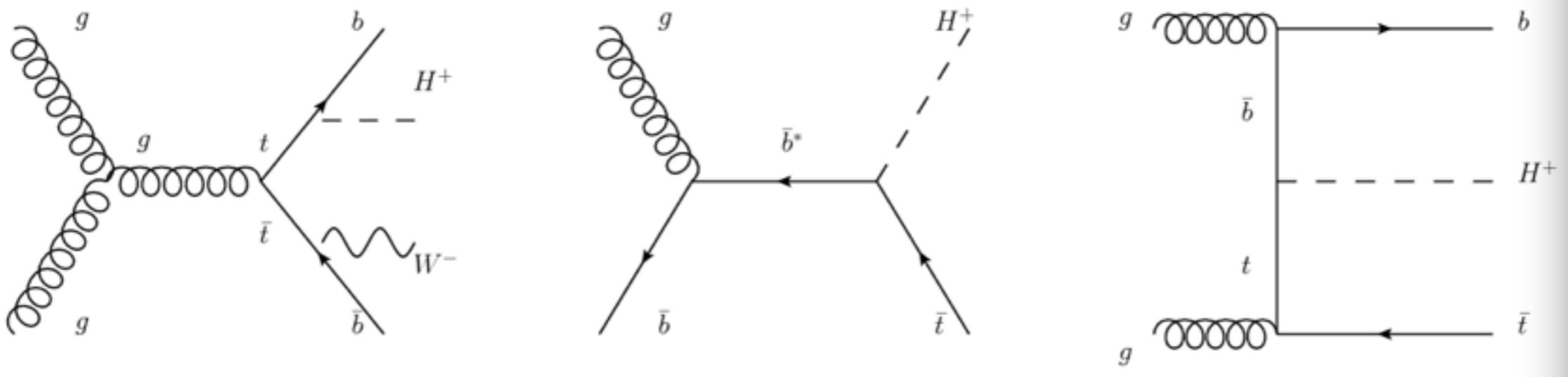
$$M > m_t + m_b \quad gb \rightarrow tH^-$$

Kunszt et.al 1992

Gunion et.al(1987), Barnett et.al (1988),  
Barger et.al (1994), Miller et.al (2000)...

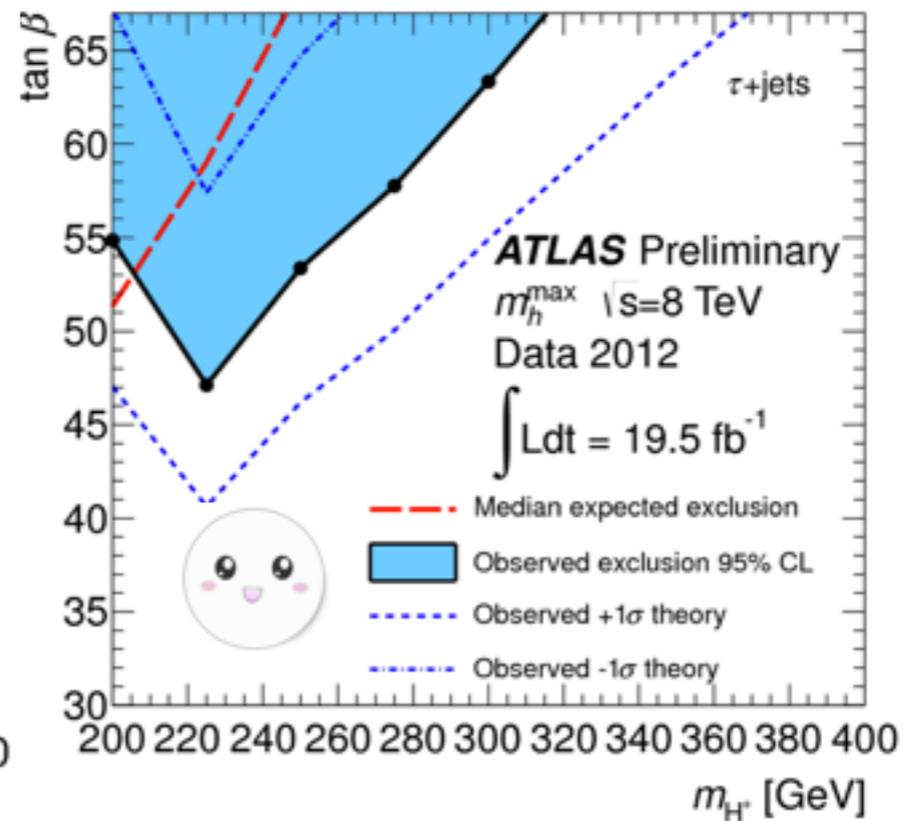
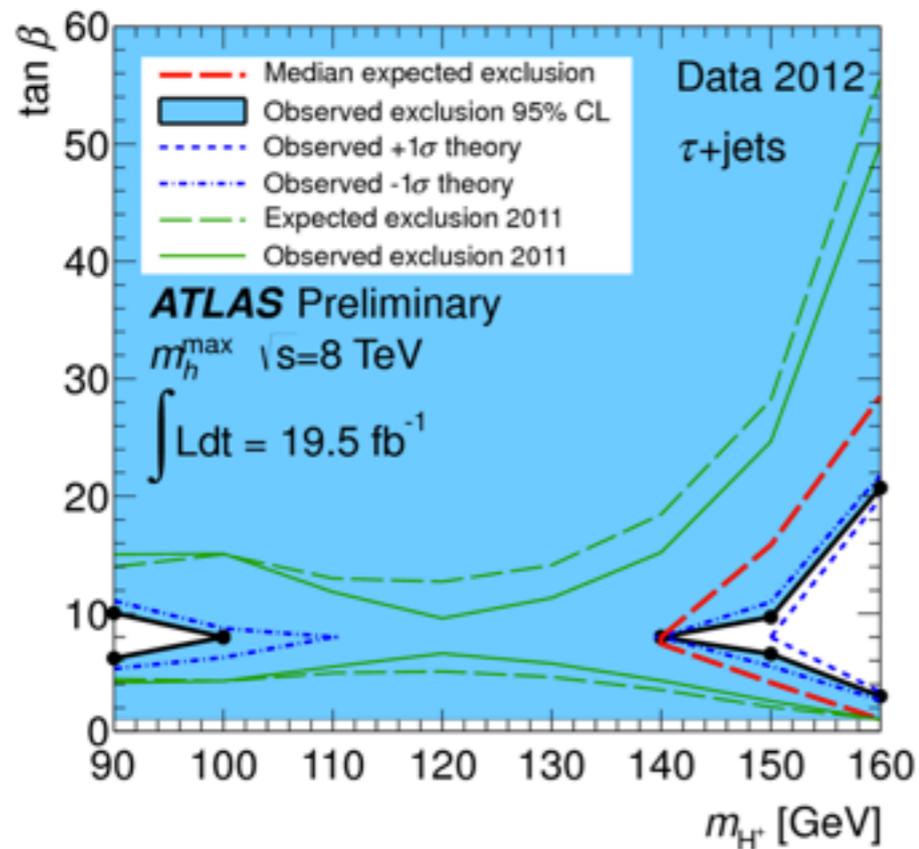
# Search for extra Higgs bosons at ILC after LHC

## Collider constraints on charged Higgs boson



$H \rightarrow \tau \nu$

$\tau$  jets  
final  
states

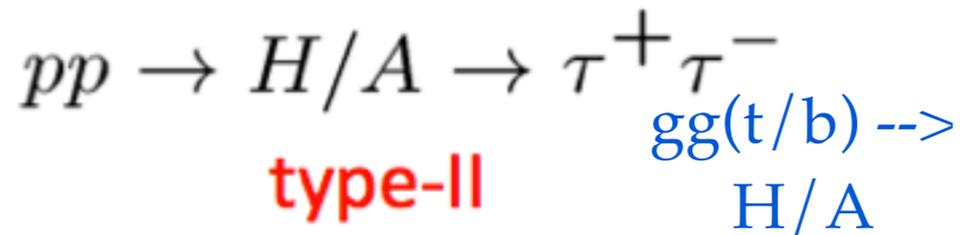


ATLAS-CONF-2013-090

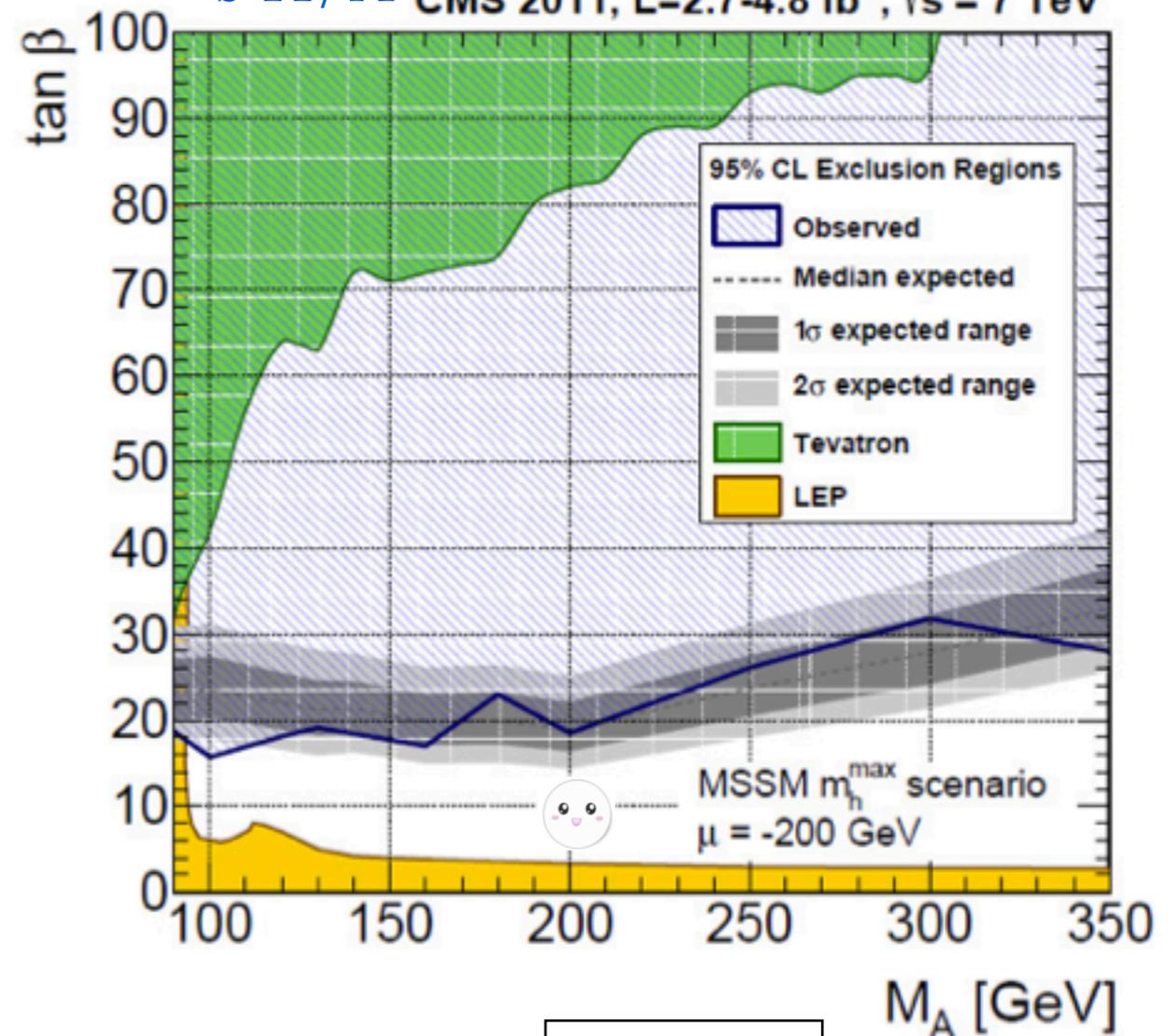
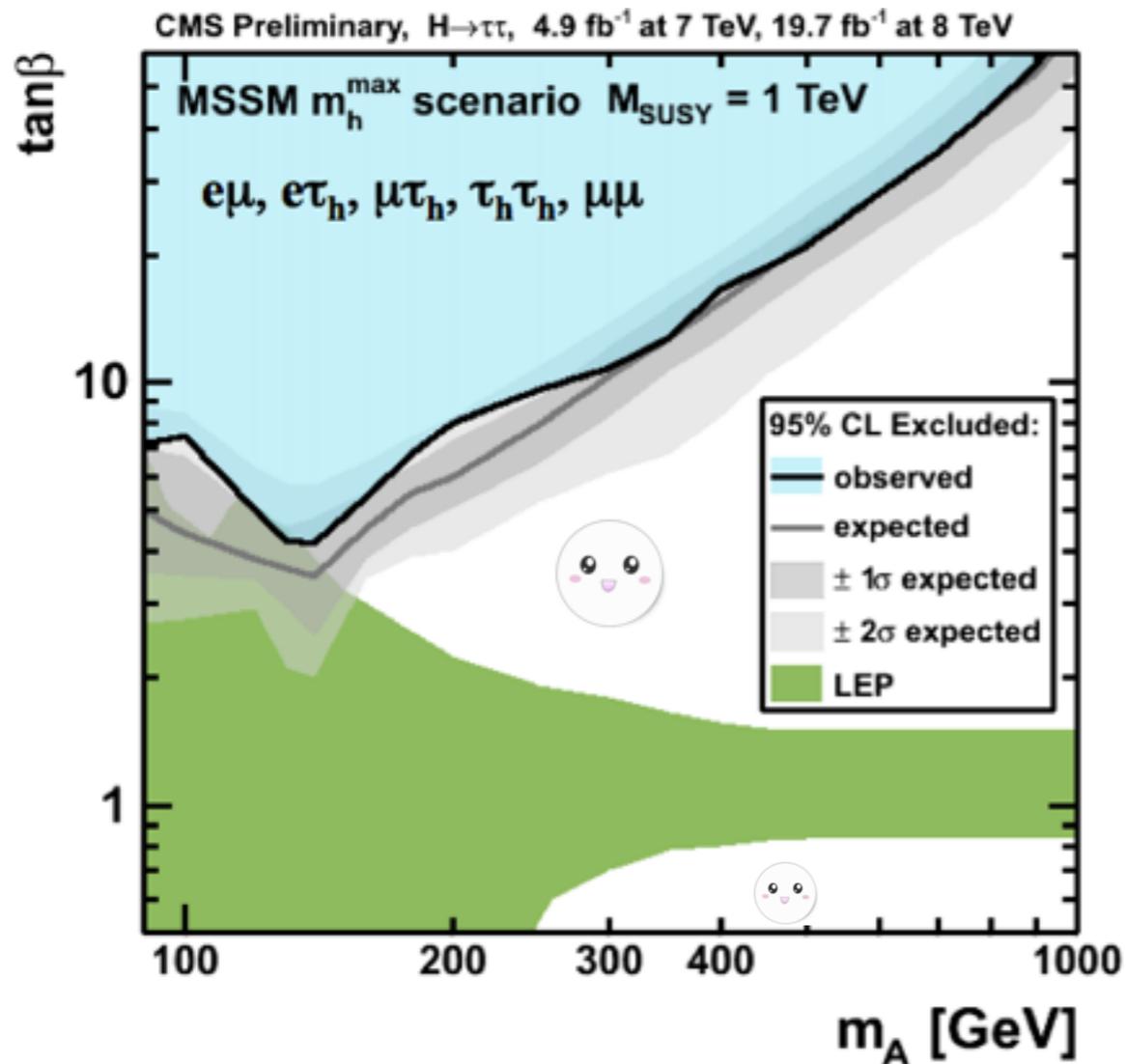
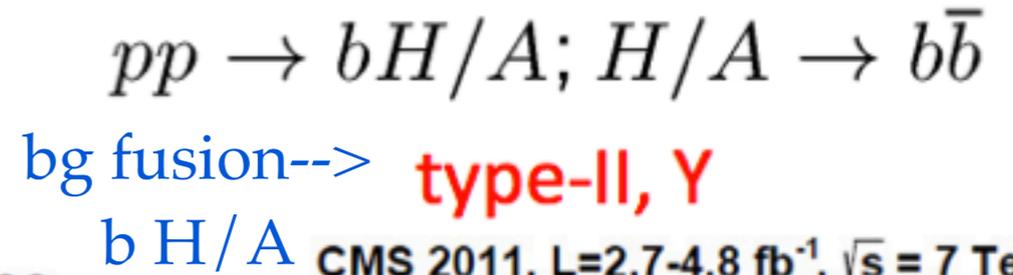
CMS: light Higgs region

# Search for extra Higgs bosons at ILC after LHC

## Collider constraints on neutral Higgs boson



	$\Phi_1$	$\Phi_2$	$w_R$	$d_R$	$\ell_R$	$Q_L$	$L_L$
Type-I	+	-	-	-	-	+	+
Type-II	+	-	-	+	+	+	+
Type-X	+	-	-	-	+	+	+
Type-Y	+	-	-	+	-	+	+



HIG-13-021

HIG-12-033

No constraint so far on Type I and Type X

# Search for extra Higgs bosons at ILC after LHC

## Higgs Decay

partial decay width:

$$\Gamma(\varphi \rightarrow q\bar{q}) = N_C \frac{G_F m_\varphi m_q^2}{4\sqrt{2}\pi} \xi_\varphi^{q2} \times \begin{cases} \beta_q^3 & \text{for } \varphi = h, H \\ \beta_q & \text{for } \varphi = A \end{cases},$$

$$\Gamma(\varphi \rightarrow \ell^+ \ell^-) = \frac{G_F m_\varphi m_\ell^2}{4\sqrt{2}\pi} \xi_\varphi^{\ell 2} \times \begin{cases} \beta_\ell^3 & \text{for } \varphi = h, H \\ \beta_\ell & \text{for } \varphi = A \end{cases},$$

$$\Gamma(H^\pm \rightarrow \underline{u}\bar{d}) = N_C \frac{G_F m_{H^\pm} |V_{ud}|^2}{4\sqrt{2}\pi} \beta_{ud} \left\{ \left( m_u^2 \xi_A^{u2} + m_d^2 \xi_A^{d2} \right) \left( 1 - \frac{m_u^2 + m_d^2}{m_{H^\pm}^2} \right) - \frac{4m_u^2 m_d^2 \xi_A^u \xi_A^d}{m_{H^\pm}^2} \right\},$$

$$\Gamma(H^\pm \rightarrow \ell^+ \nu) = \frac{G_F m_{H^\pm} m_\ell^2}{4\sqrt{2}\pi} \xi_A^{\ell 2} \left( 1 - \frac{m_\ell^2}{m_{H^\pm}^2} \right)^2,$$

$$\lambda(x, y) = 1 + x^2 + y^2 - 2x - 2y - 2xy,$$

$$q = u, d, s, c, t, b; \ell = e, \mu, \tau;$$

$$\beta_X = \lambda^{1/2} \left( \frac{m_X^2}{m_\varphi^2}, \frac{m_X^2}{m_\varphi^2} \right) = \sqrt{1 - \frac{4m_X^2}{m_\varphi^2}},$$

$$\beta_{XY} = \lambda^{1/2} \left( \frac{m_X^2}{m_\varphi^2}, \frac{m_Y^2}{m_\varphi^2} \right).$$

$N_c=3$  is color factor;  $V_{ud}$ : KM matrix

## Higgs decay

partial decay width:

$$\Gamma(\varphi \rightarrow gg) = \frac{G_F \alpha_S^2 m_\varphi^3}{64 \sqrt{2} \pi^3} \left| \sum_{f=q} I_f^\varphi(m_f, 1) \right|^2$$

$$\Gamma(\varphi \rightarrow \gamma\gamma) = \frac{G_F \alpha_{EM}^2 m_\varphi^3}{128 \sqrt{2} \pi^3} \left| \sum_f Q_f^2 I_f^\varphi(m_f, N_C) + I_W^\varphi + I_{H^\pm}^\varphi \right|^2$$

where fermionic loop functions are given by

$$I_f^\varphi(m_f, N_C) = \xi_\varphi^f \times \begin{cases} -N_C \frac{4m_f^2}{m_\varphi^2} [2 - \beta_f^2 m_\varphi^2 C_0(0, 0, m_\varphi^2, m_f^2, m_f^2, m_f^2)] & \text{for } \varphi = h, H \\ +4N_C m_f^2 C_0(0, 0, m_\varphi^2, m_f^2, m_f^2, m_f^2) & \text{for } \varphi = A \end{cases}$$

Passarino-Veltman functions:

$$C_0(0, 0, m_\varphi^2, m^2, m^2, m^2) = \frac{-2}{m_\varphi^2} f\left(\frac{4m^2}{m_\varphi^2}\right)$$

$$f(x) = \begin{cases} \left[ \arcsin\left(\sqrt{1/x}\right) \right]^2 & \text{for } x \geq 1 \\ -\frac{1}{4} \left[ \ln\left(\frac{1+\sqrt{1-x}}{1-\sqrt{1-x}}\right) - i\pi \right]^2 & \text{for } x < 1 \end{cases}$$

Aoki, Kanemura, Tsumura and Yagyu, 2009

Gunion, Haber, Kane and Dawson, 1990

Djouadi, Phys. Rept. 2008

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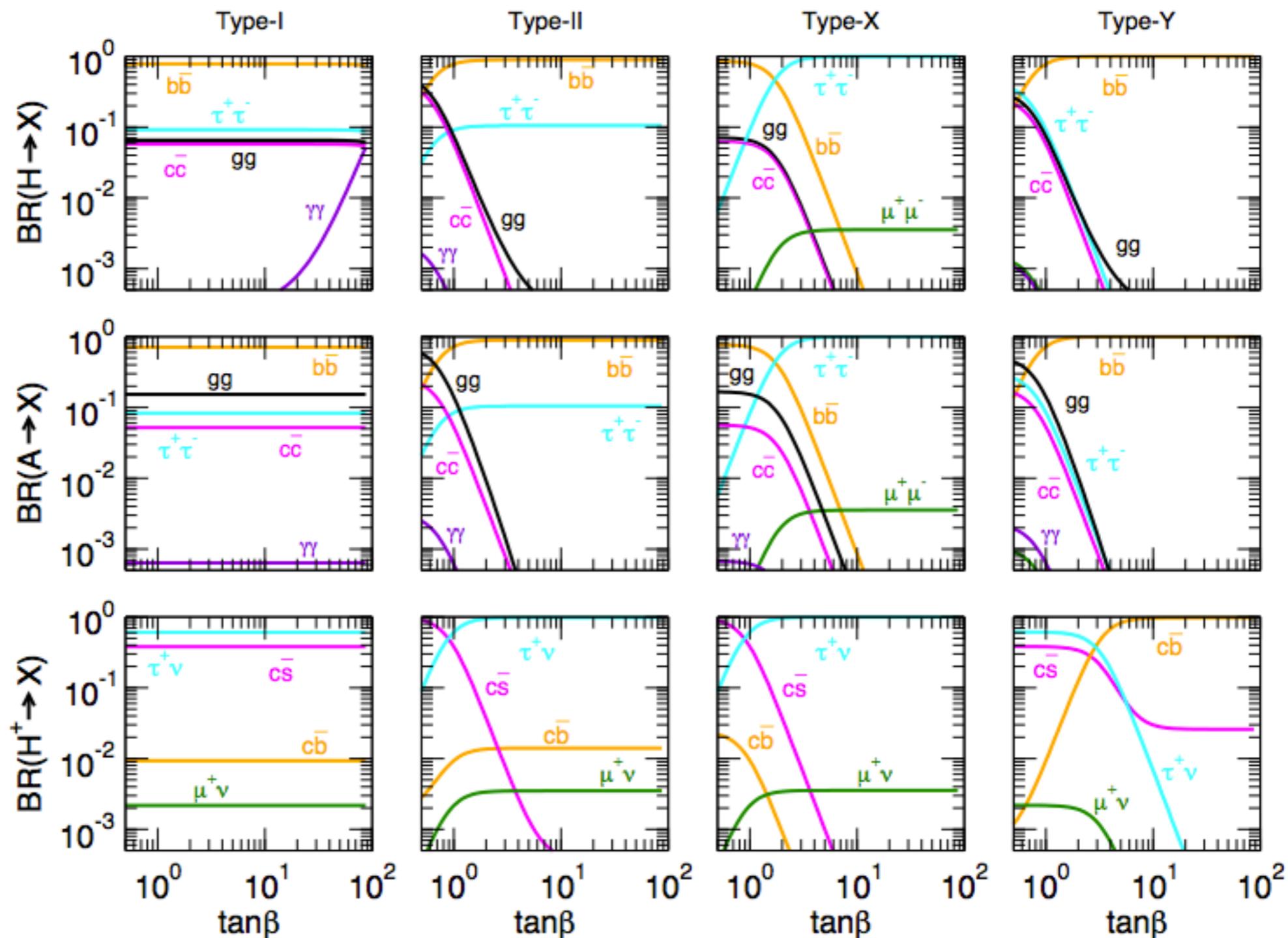
## Higgs decay branching ratio

125 GeV Higgs

SM-like limit

$$m_H = m_A = m_{H^\pm}$$

$$\sin(\beta - \alpha) = 1$$



# Search for extra Higgs bosons at ILC after LHC

## Higgs decay branching ratio

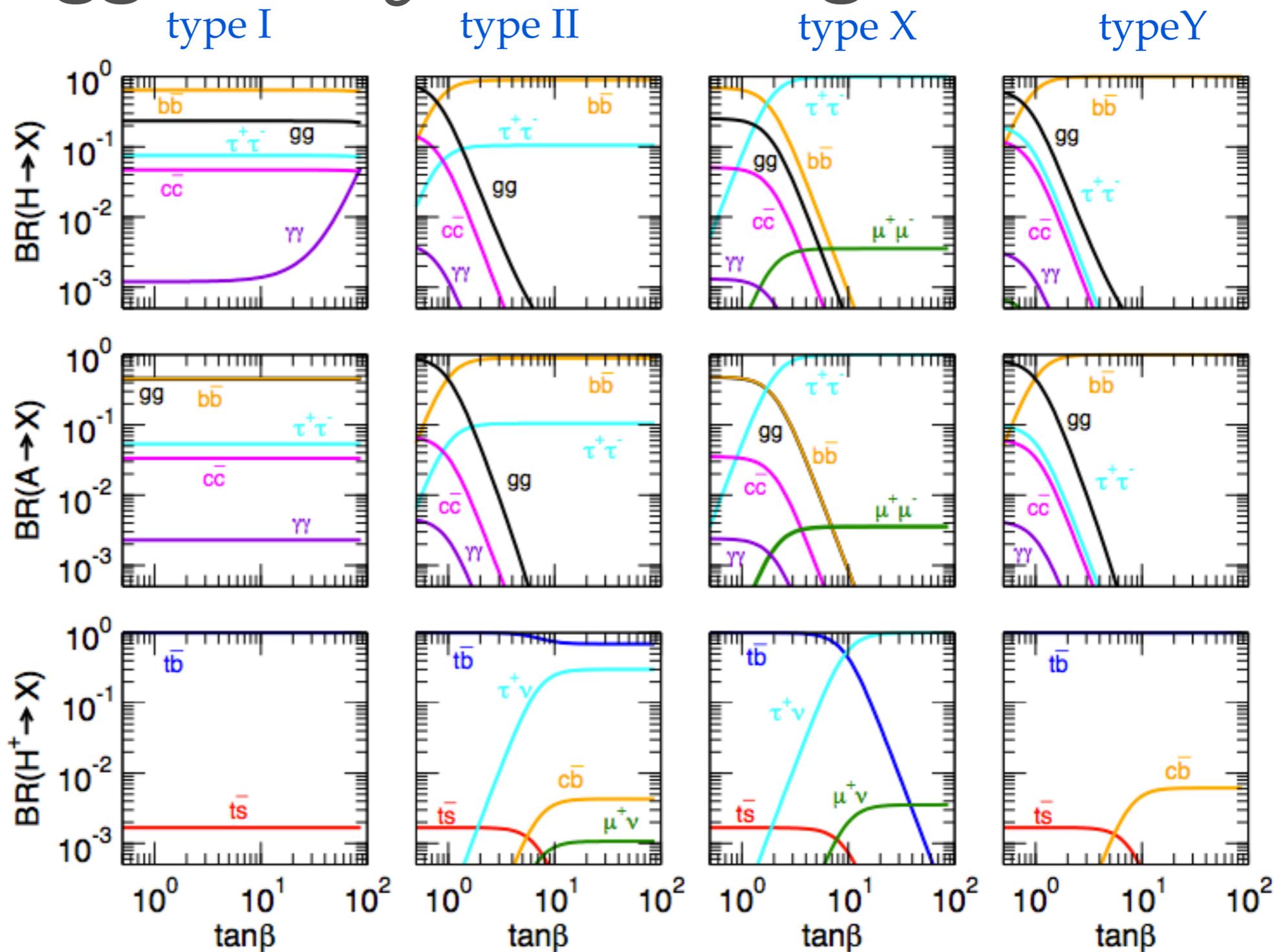
250 GeV Higgs

SM-like limit

$$m_H = m_A = m_{H^\pm}$$

$$\sin(\beta - \alpha) = 1$$

H to top decay  
open



# Search for extra Higgs bosons at ILC after LHC

## Higgs decay branching ratio

type I

type II

type X

type Y

500 GeV Higgs

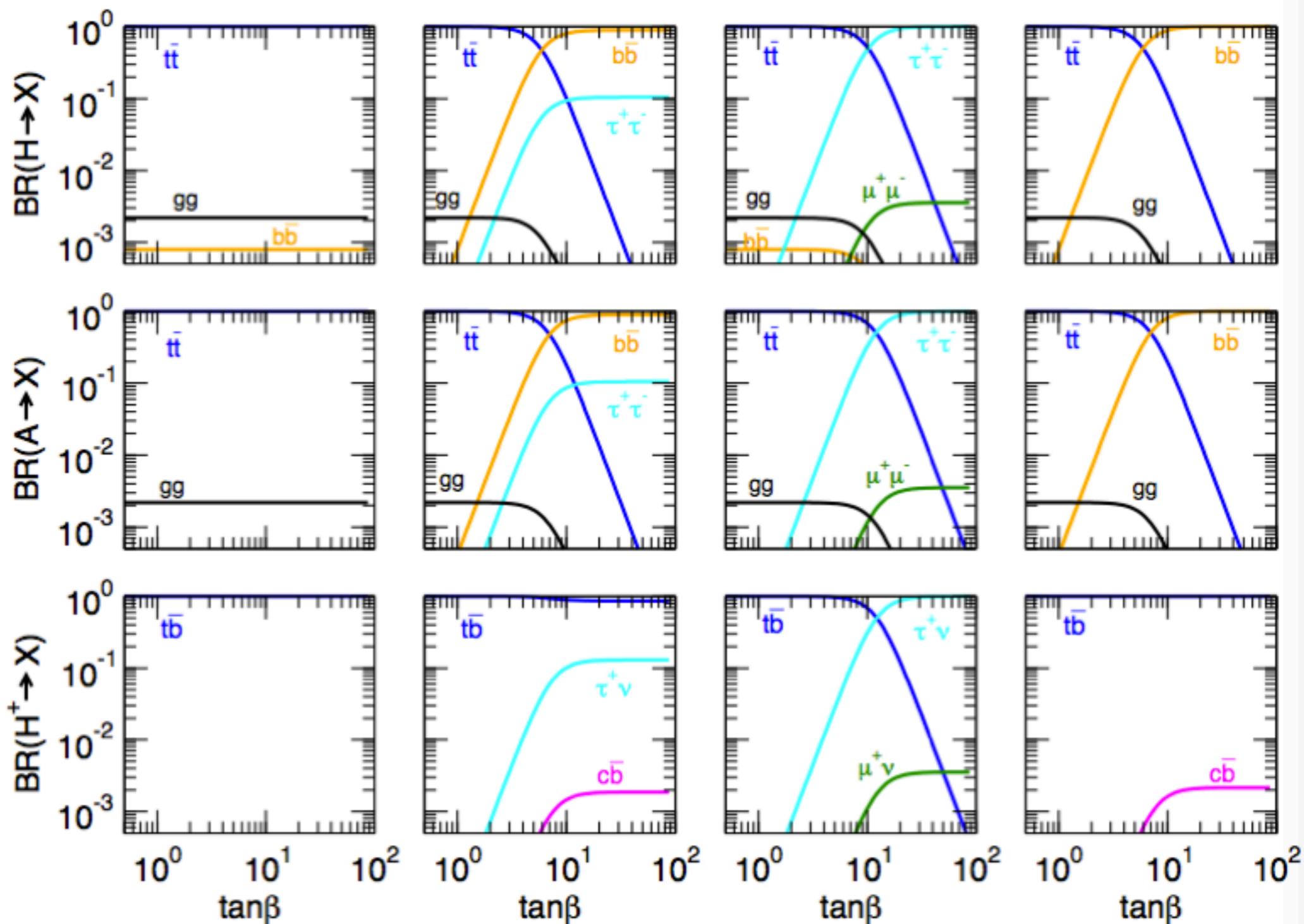
SM-like limit

$$m_H = m_A = m_{H^\pm}$$

$$\sin(\beta - \alpha) = 1$$

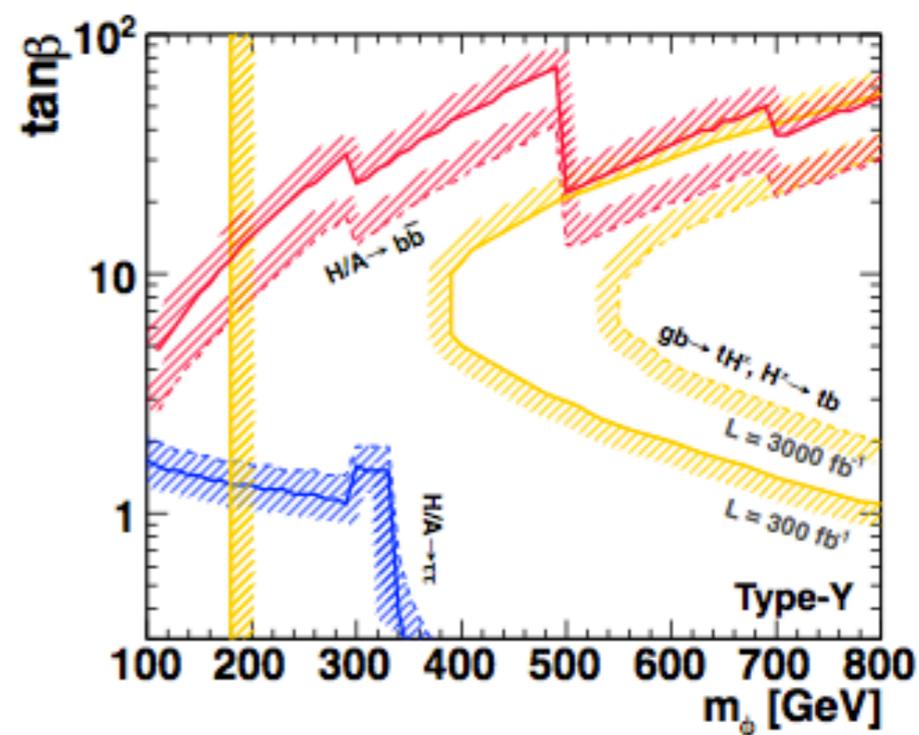
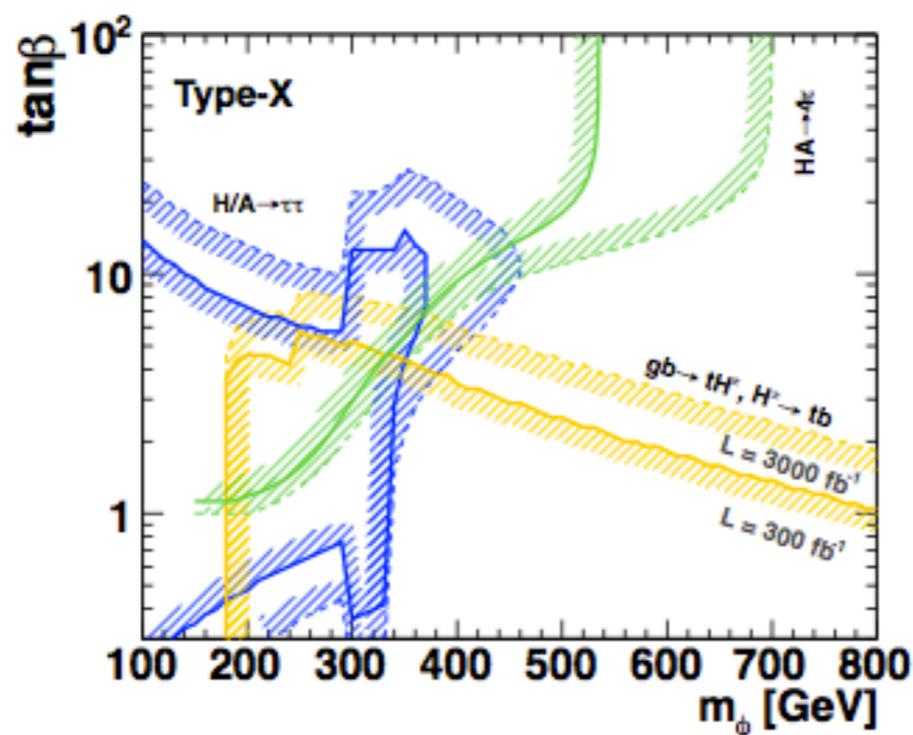
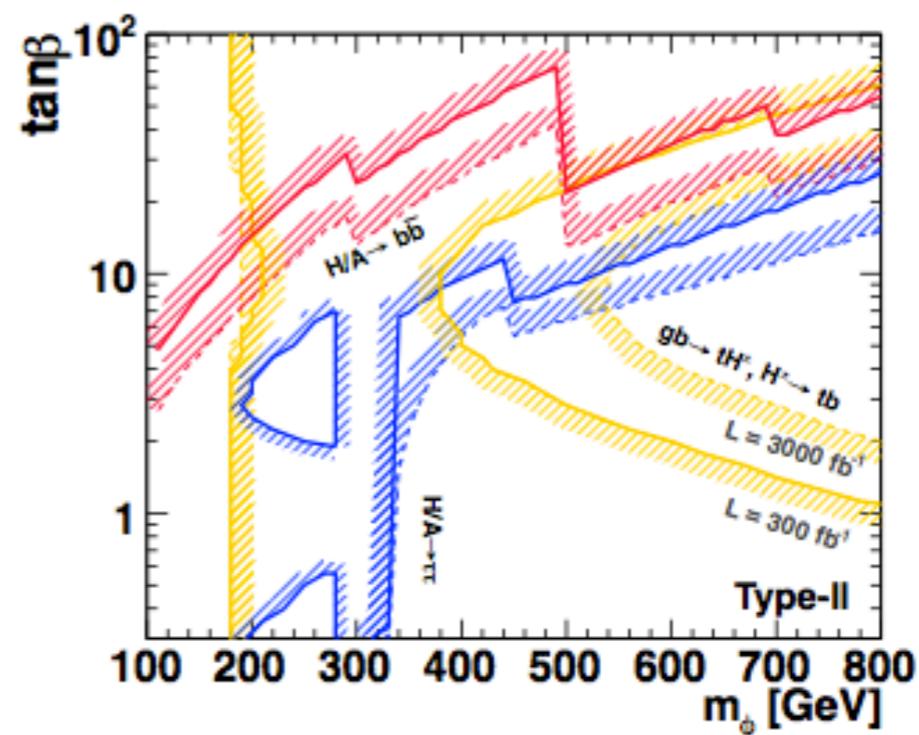
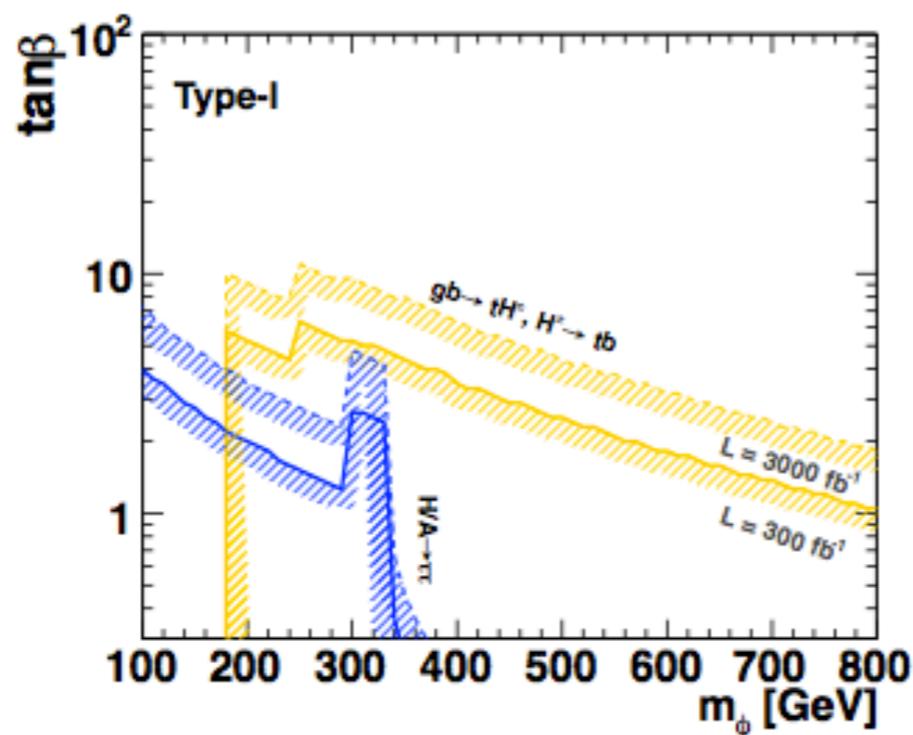
H to top decay  
open

go beyond the  
threshold of pair  
production  
and we can  
study the single  
production with  
different decay  
channels



# Search for extra Higgs bosons at ILC after LHC

2 sigma exclusion regions (theoretical prediction)



# Search for extra Higgs bosons at ILC after LHC

## Higgs Production process at ILC

$\sqrt{s} < 2M$

below the pair production  
mass threshold

$$e^-e^+ \rightarrow \tau^- \bar{\nu}_\tau H^+, \tau^+ \nu_\tau H^-$$

$$e^-e^+ \rightarrow \bar{t}bH^+, t\bar{b}H^-$$

$$e^+e^- \rightarrow b\bar{b}H/A$$

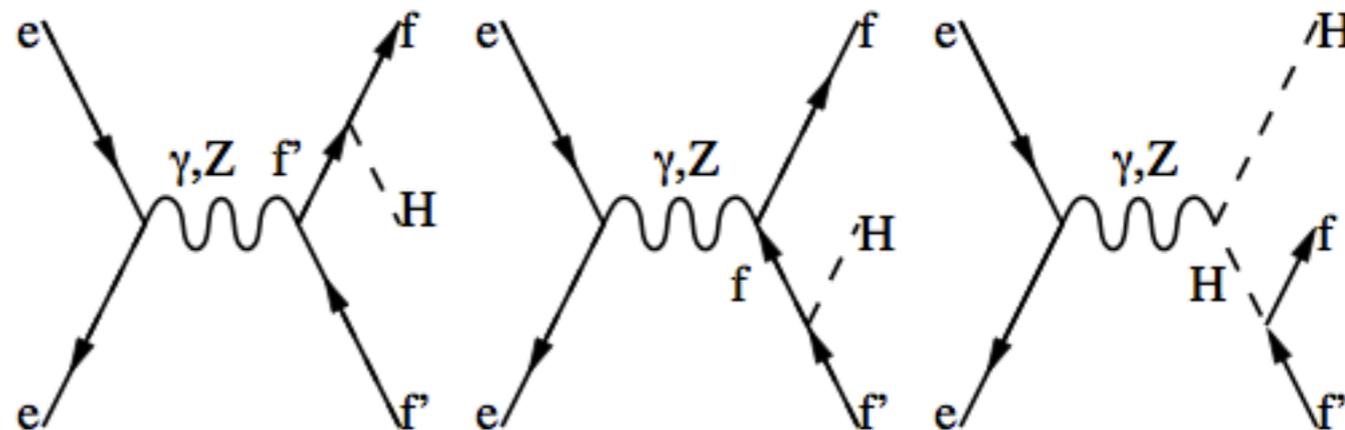
$$e^+e^- \rightarrow \tau^+\tau^-H/A$$

$\sqrt{s} > 2M$

above the pair production  
mass threshold

$$e^+e^- \rightarrow H^+H^- / HA$$

- $e^-e^+ \rightarrow \bar{t}bH^+, t\bar{b}H^-$
- $e^-e^+ \rightarrow W^\mp H^\pm$  (one loop)
- $e^-e^+ \rightarrow e^- \bar{\nu}_e H^+, e^+ \nu_e H^-$  (one loop)
- $e^-e^+ \rightarrow Z^0 W^\mp H^\pm$
- $e^-e^+ \rightarrow h^0 W^\mp H^\pm$
- $e^-e^+ \rightarrow H^0 W^\mp H^\pm$
- $e^-e^+ \rightarrow A^0 W^\mp H^\pm$
- $e^-e^+ \rightarrow e^- e^+ W^\mp H^\pm$
- $e^-e^+ \rightarrow \nu_e \bar{\nu}_e W^\mp H^\pm$
- $e^-e^+ \rightarrow e^- \bar{\nu}_e Z^0 H^+, e^+ \nu_e Z^0 H^-$
- $e^-e^+ \rightarrow e^- \bar{\nu}_e h^0 H^+, e^+ \nu_e h^0 H^-$
- $e^-e^+ \rightarrow e^- \bar{\nu}_e H^0 H^+, e^+ \nu_e H^0 H^-$
- $e^-e^+ \rightarrow e^- \bar{\nu}_e A^0 H^+, e^+ \nu_e A^0 H^-$



type II 2HDM study :

Kanemura et.al, (2001), Moretti(2002)

thorough study on Higgs production with all  
types of Yukawa interactions at LO

# Search for extra Higgs bosons at ILC after LHC

neutral Higgs

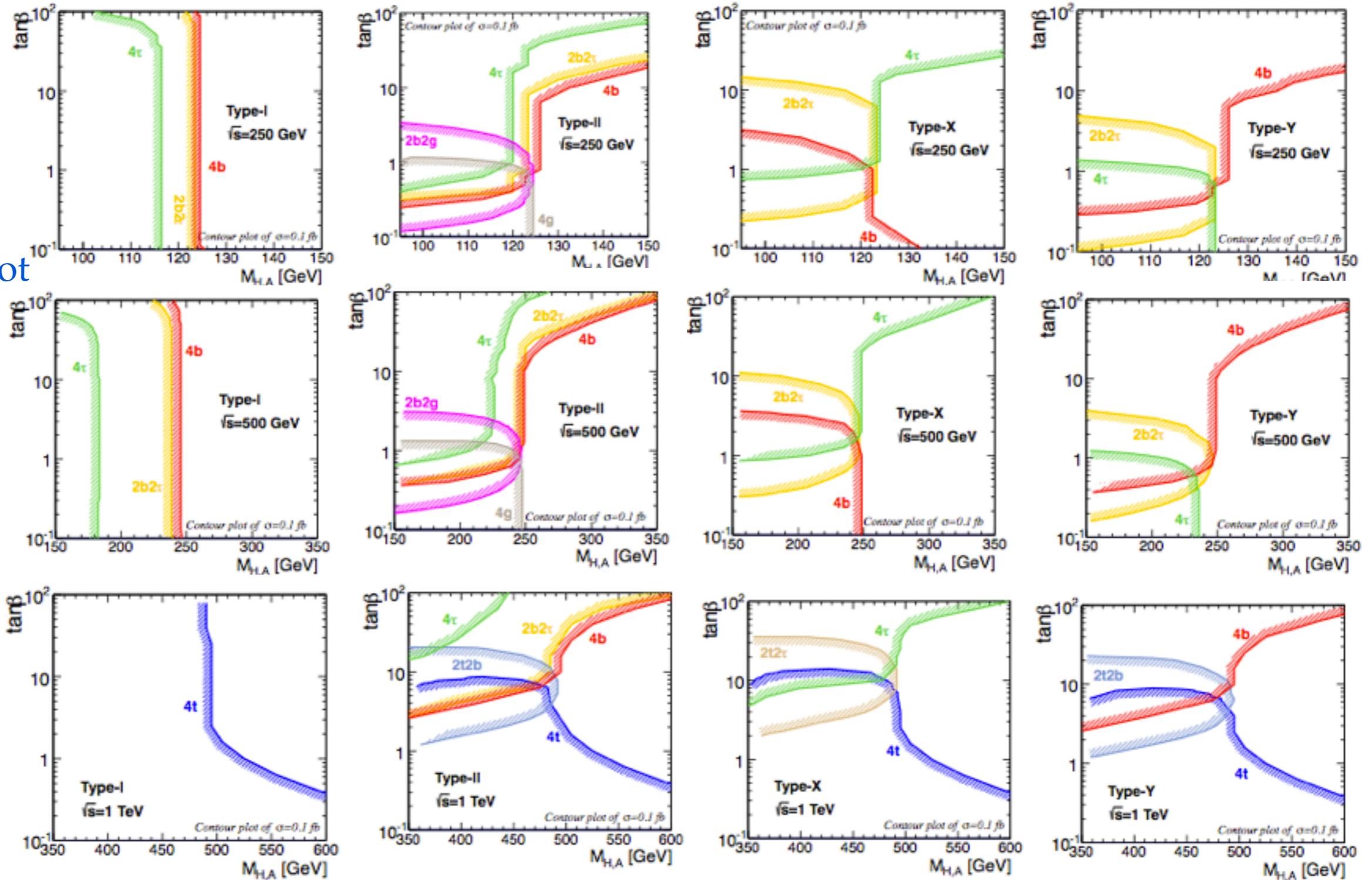
type I

type II

type X

type Y

0.1fb  
contour plot



sensitive to different types

# Search for extra Higgs bosons at ILC after LHC

Charged Higgs

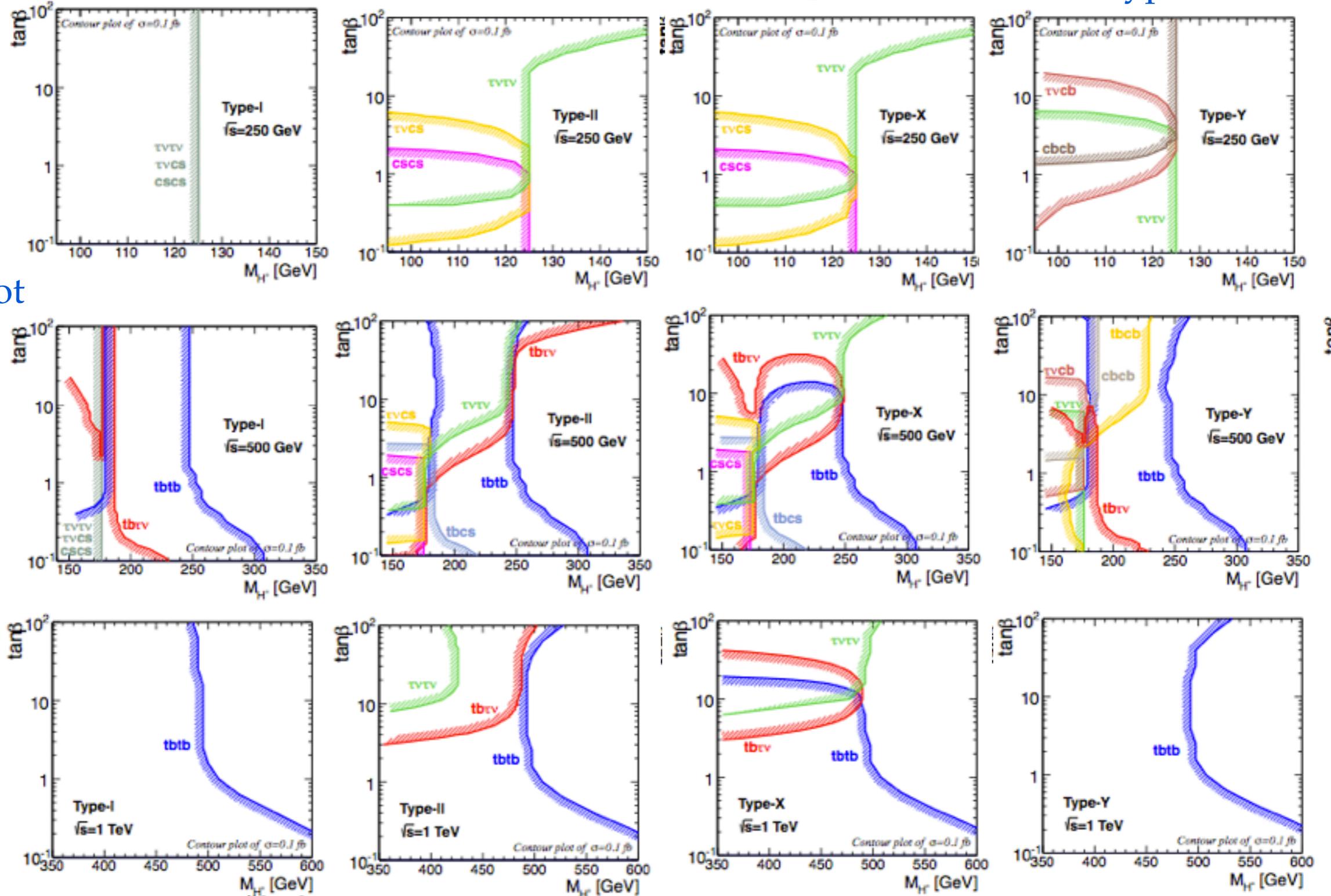
type I

type II

type X

type Y

0.1fb  
contour plot



## SM background

Signature	$\sqrt{s} = 250$ GeV	$\sqrt{s} = 500$ GeV	$\sqrt{s} = 1$ TeV
$4b$	18	7.2	2.9
$4\tau$	4.4	1.6	0.63
$2\tau 2b$	28	10	3.5
$2\tau 2\nu$	210	94.4	35.8
$tb\tau\nu$	$5.7 \times 10^{-4}$	122.7	40
$2t2b$	—	1.7	5.1
$2t2\tau$	—	0.14	0.34
$4t$	—	—	$1.4 \times 10^{-3}$

TABLE III: Background cross sections in unit of fb for the four-particle processes at the ILC. Total cross sections without kinematical cuts are calculated by Madgraph [123].

without kinematic cuts

# Search for extra Higgs bosons at ILC after LHC

## Benchmark scenarios

$(m_\phi, \tan \beta)$		Type-I		Type-II		Type-X		Type-Y	
		$H, A$	$H^\pm$	$H, A$	$H^\pm$	$H, A$	$H^\pm$	$H, A$	$H^\pm$
(220 GeV, 20)	LHC300	—	—	$\tau\tau, bb$	$tb$	$4\tau$	—	$bb$	$tb$
	LHC3000	—	—	$\tau\tau, bb$	$tb$	$4\tau$	—	$bb$	$tb$
	ILC500	$4b, 2b2\tau, 4g,$ $2b2g, 2\tau2g$	$tbtb$	$4b, 2b2\tau, tbtb, tb\tau\nu,$ $4\tau$	$\tau\nu\tau\nu$	$4\tau$	$tb\tau\nu,$ $\tau\nu\tau\nu$	$4b$	$tbtb, tbc b$
(220 GeV, 7)	LHC300	—	—	$\tau\tau$	$tb$	$4\tau$	—	—	$tb$
	LHC3000	—	$tb$	$\tau\tau$	$tb$	$\tau\tau, 4\tau$	—	—	$tb$
	ILC500	$4b, 2b2\tau, 4g,$ $2b2g, 2\tau2g$	$tbtb$	$4b, 2b2\tau, tbtb, tb\tau\nu,$ $4\tau$	$\tau\nu\tau\nu$	$2b2\tau, 4\tau$	$tbtb, tb\tau\nu,$ $\tau\nu\tau\nu$	$4b$	$tbtb, tbc b$
(220 GeV, 2)	LHC300	—	$tb$	$\tau\tau$	$tb$	$\tau\tau, 4\tau$	$tb$	—	$tb$
	LHC3000	$\tau\tau$	$tb$	$\tau\tau$	$tb$	$\tau\tau, 4\tau$	$tb$	—	$tb$
	ILC500	$4b, 2b2\tau, 4g,$ $2b2g, 2\tau2g$	$tbtb$	$4b, 2b2\tau,$ $4\tau, 2b2g$	$tbtb,$ $tb\tau\nu$	$4b, 2b2\tau,$ $4\tau$	$tbtb,$ $tb\tau\nu$	$4b, 2b2\tau,$ $2b2g$	$tbtb$

## Benchmark scenarios

$(m_\phi, \tan \beta)$		Type-I		Type-II		Type-X		Type-Y	
		$H, A$	$H^\pm$	$H, A$	$H^\pm$	$H, A$	$H^\pm$	$H, A$	$H^\pm$
(400 GeV, 20)	LHC300	–	–	$\tau\tau$	$tb$	$4\tau$	–	–	$tb$
	LHC3000	–	–	$\tau\tau$	$tb$	$\tau\tau, 4\tau$	–	–	$tb$
	ILC1TeV	$4t$	$tbtb$	$4b, 2b2\tau, 2t2b$	$tbtb, tb\tau\nu, \tau\nu\tau\nu$	$4\tau, 2t2\tau$	$tb\tau\nu, \tau\nu\tau\nu$	$4b, 2t2b$	$tbtb$
(400 GeV, 7)	LHC300	–	–	–	–	–	–	–	–
	LHC3000	–	–	$\tau\tau$	$tb$	$\tau\tau, 4\tau$	–	–	$tb$
	ILC1TeV	$4t$	$tbtb$	$4b, 2b2\tau, 2t2b, 4t$	$tbtb, tb\tau\nu$	$4t, 2t2\tau$	$tbtb, tb\tau\nu$	$4b, 2t2b, 4t$	$tbtb$
(400 GeV, 2)	LHC300	–	$tb$	–	$tb$	–	$tb$	–	$tb$
	LHC3000	–	$tb$	–	$tb$	–	$tb$	–	$tb$
	ILC1TeV	$4t$	$tbtb$	$4t, 2t2b$	$tbtb$	$4t$	$tbtb$	$4t, 2t2b$	$tbtb$

TABLE V: The similar table as Table IV, but for  $m_\phi = 400$  GeV. ILC1TeV represents the ILC run of 1 TeV.

## Summary

- We made a complementary study on Higgs bosons in Type I, II, X and Y 2HDMs at ILC and emphasize on the parameter region beyond LHC reach.
- Extra Higgs boson production and decay final states provides discriminative signatures from different types of Yukawa interactions within 2HDM.
- Single Higgs production above mass threshold is included and shows distinct signatures as discovery channel.

Thanks for your attention!